
Learning to Defer to a Population: A Meta-Learning Approach



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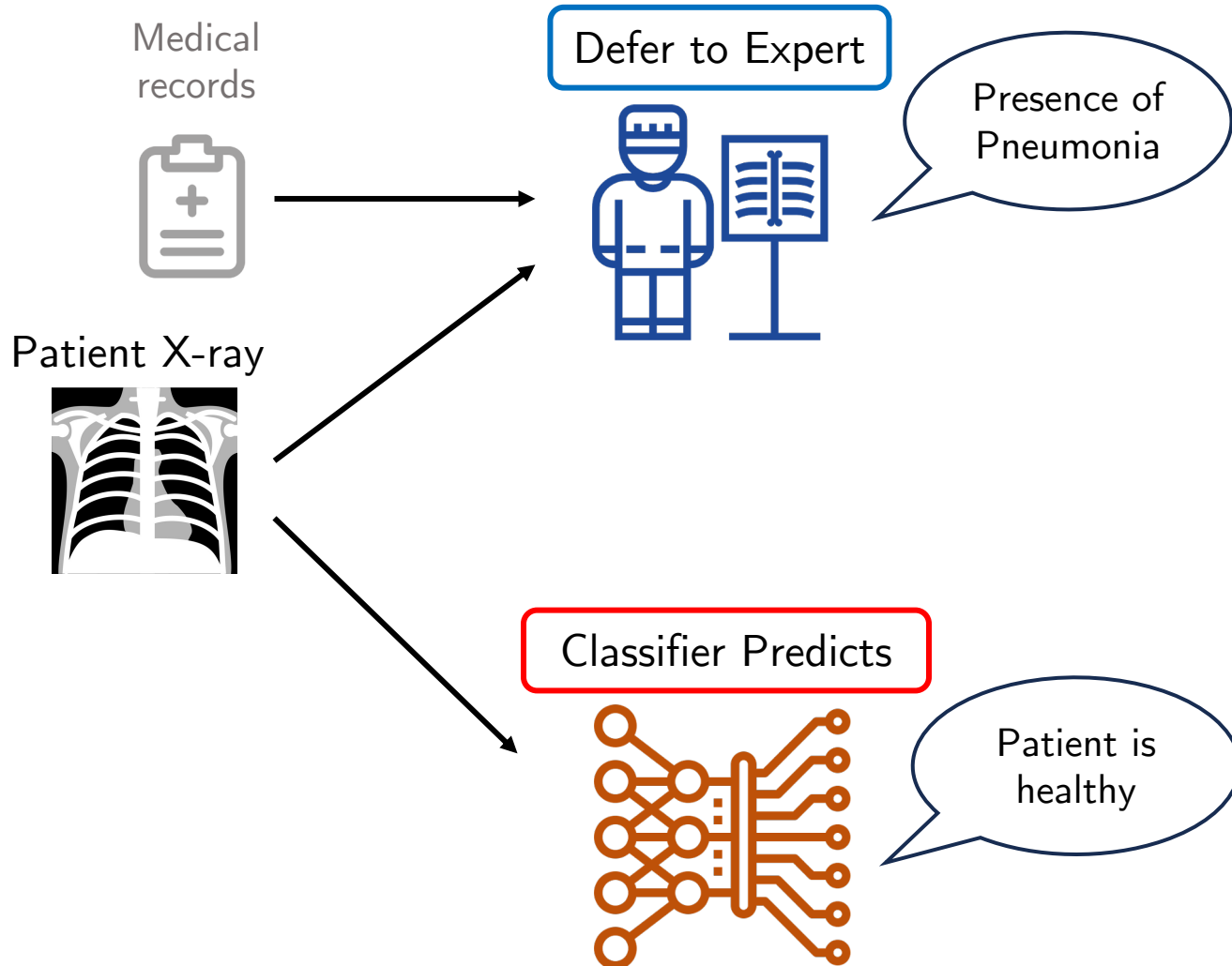


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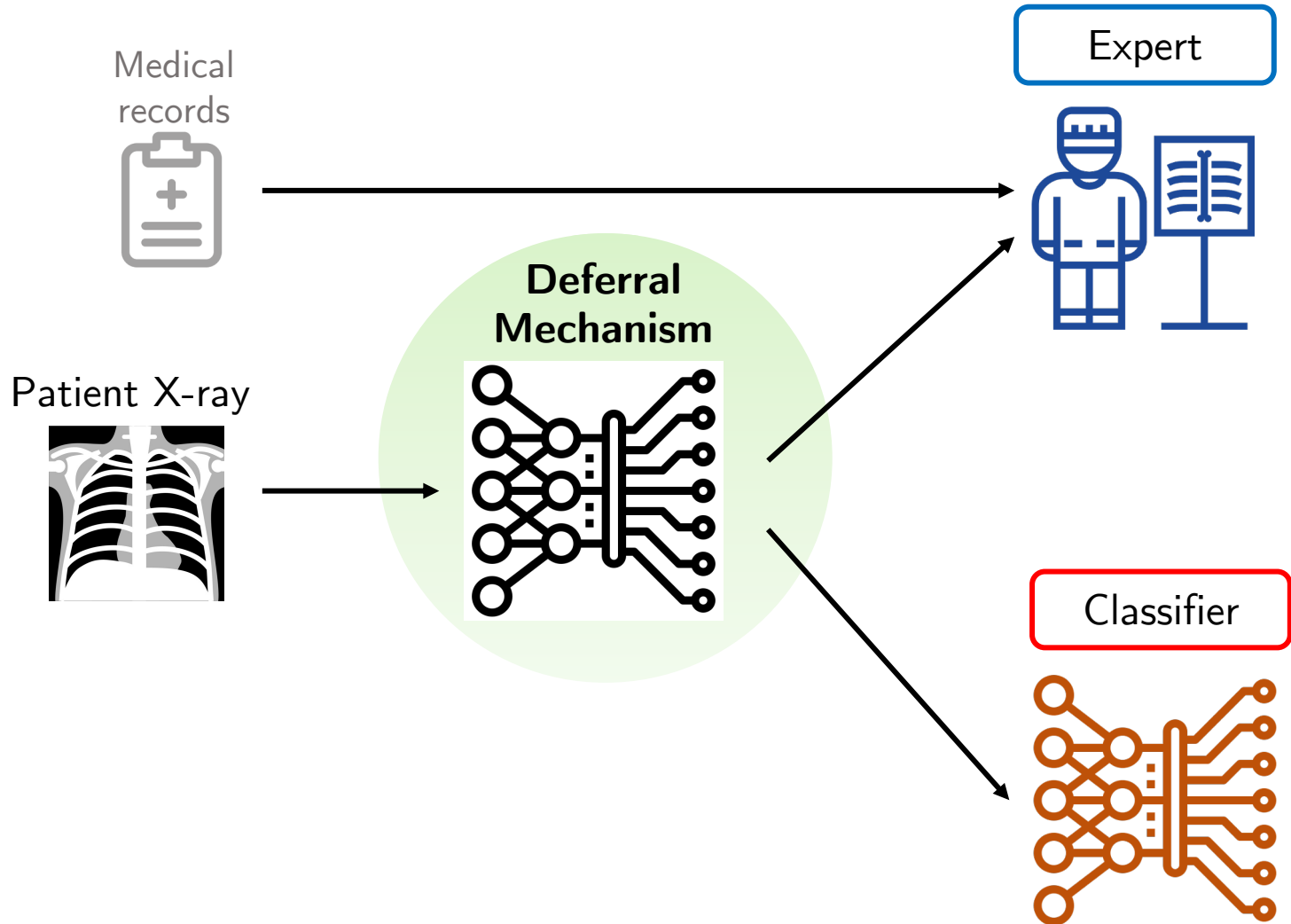
Human-AI Collaboration

Prevent critical misclassification by allocating decisions between the AI and human.



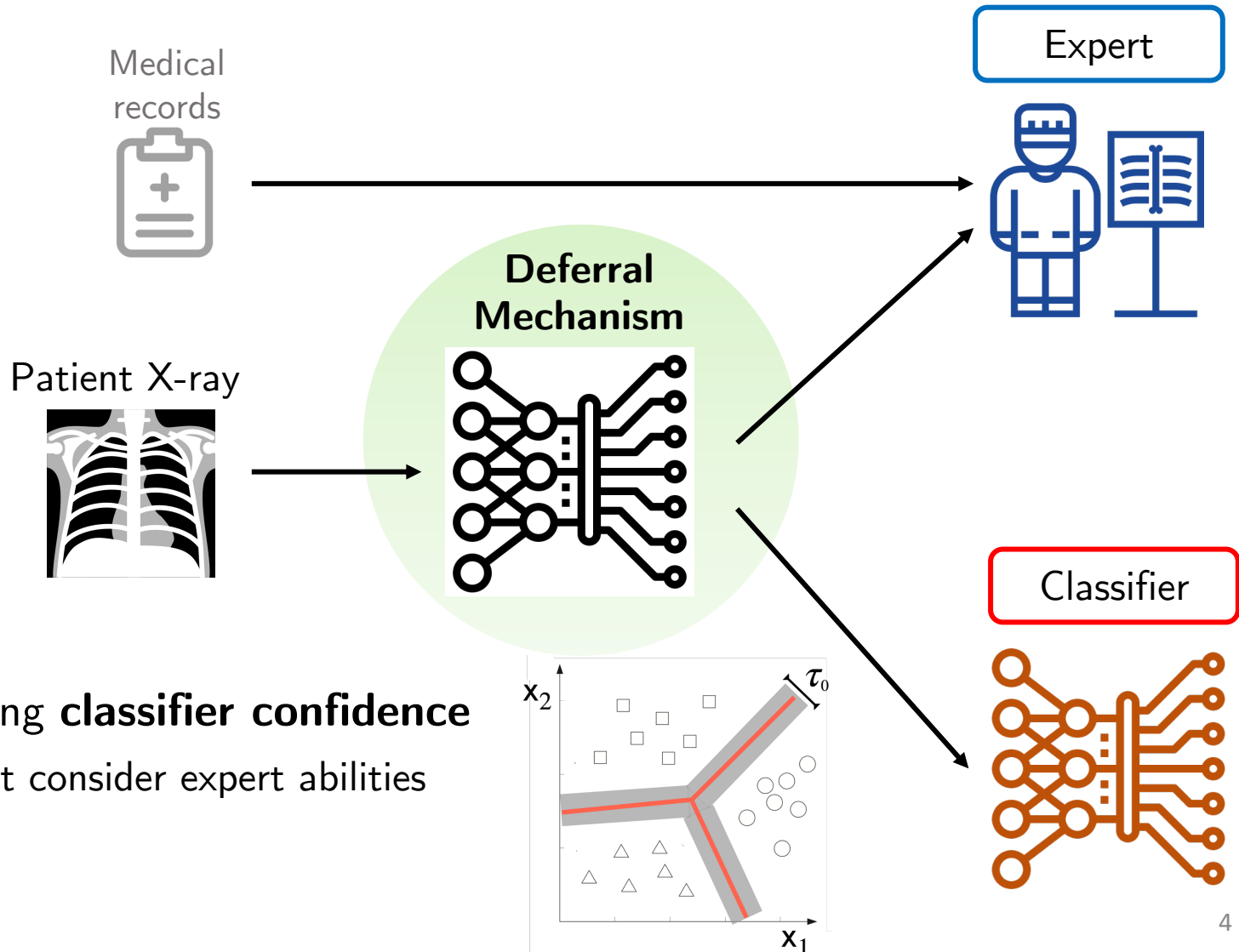
Rejection Learning

Q: How to determine which examples should be routed to the classifier or expert?



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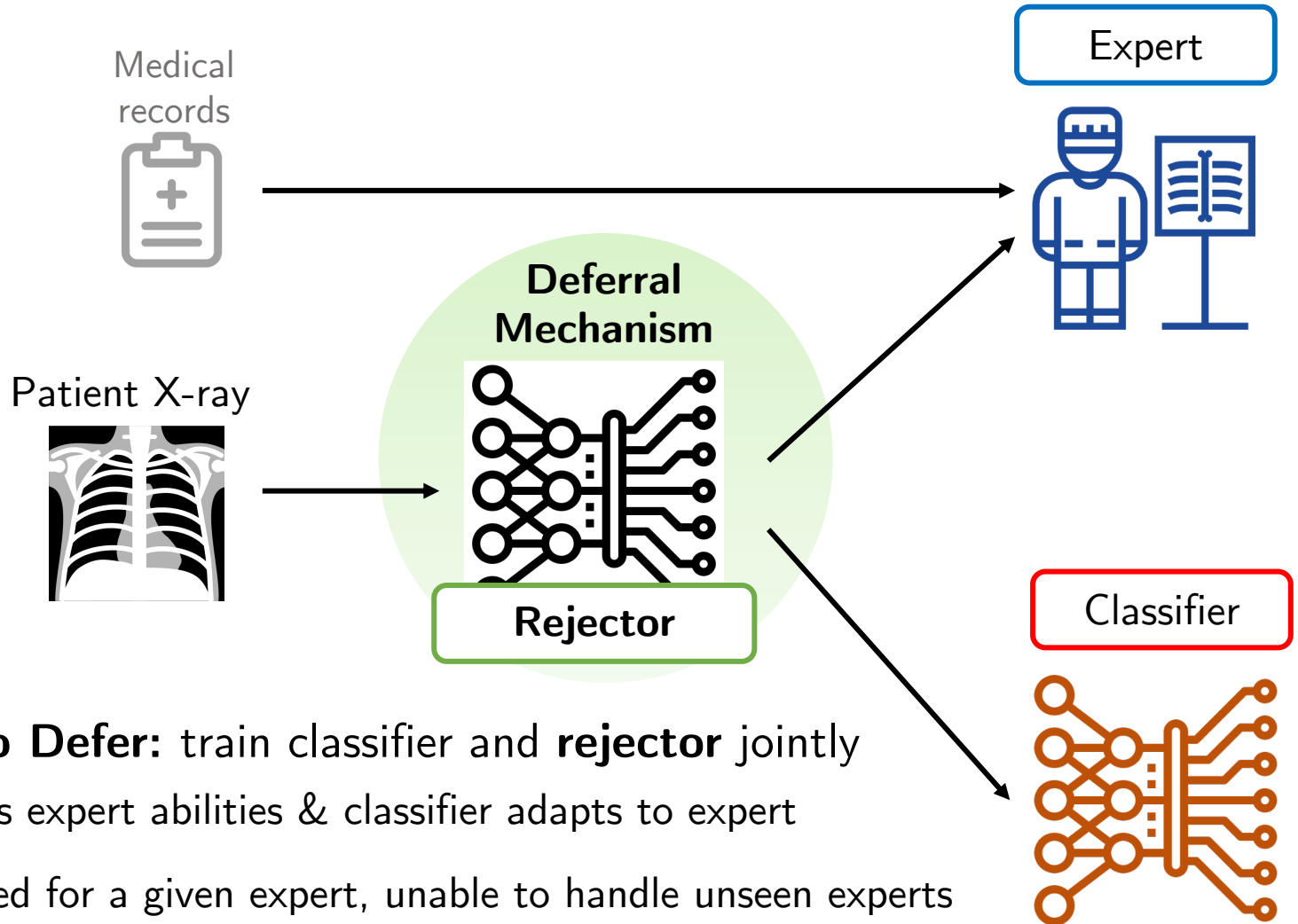


Thresholding **classifier confidence**

X Does not consider expert abilities

Rejection Learning

Q: How to determine which examples should be routed to the classifier or expert?

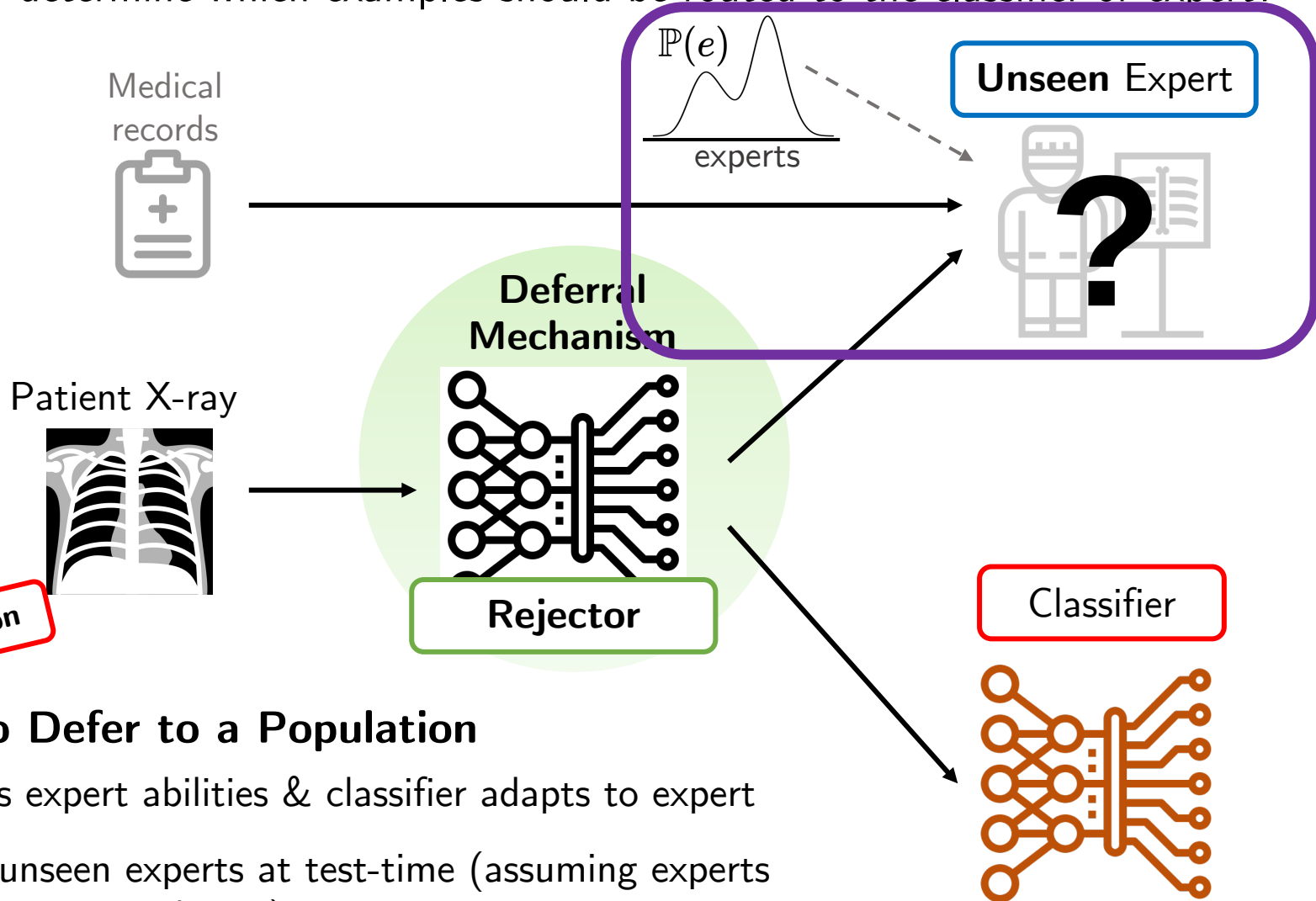


Learning to Defer: train classifier and **rejector** jointly

- ✓ Considers expert abilities & classifier adapts to expert
- ✗ Specialized for a given expert, unable to handle unseen experts

Rejection Learning

Q: How to determine which examples should be routed to the classifier or expert?



Our Contribution

Learning to Defer to a Population


- ✓ Considers expert abilities & classifier adapts to expert
- ✓ Handles unseen experts at test-time (assuming experts drawn from a population)

Learning to Defer (to a single expert)

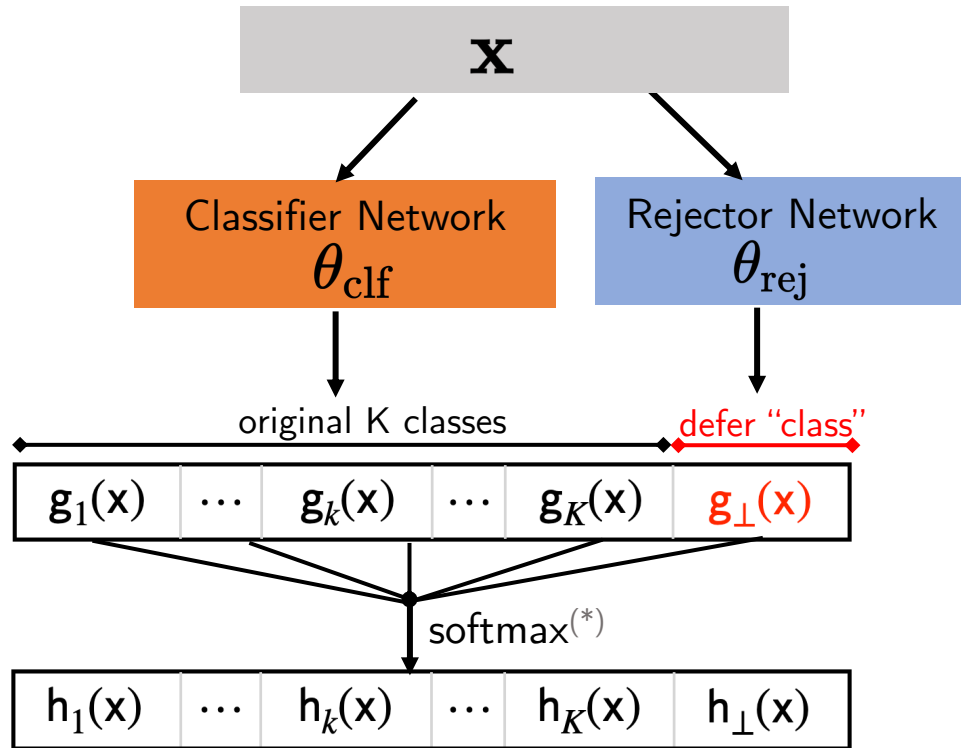
training data

$$\mathcal{D} = \{\mathbf{x}_n, y_n, m_n\}_{n=1}^N$$

expert demonstrations



Learning to Defer (to a single expert)

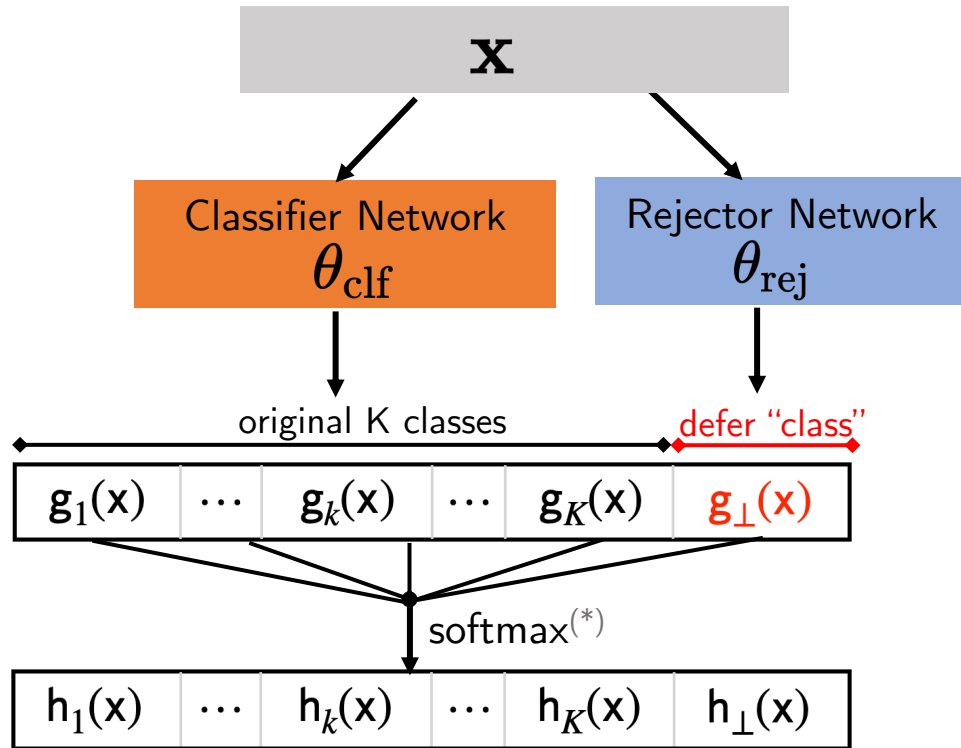


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(*) other parameterizations/surrogate losses possible

Learning to Defer (to a single expert)



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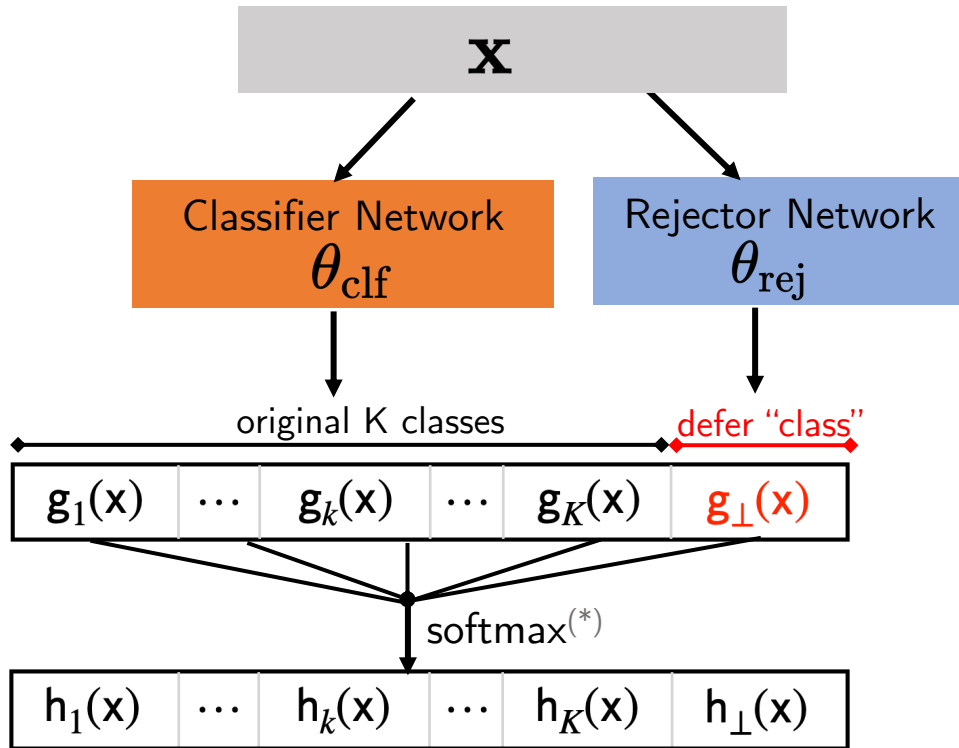
expert demonstrations

reject if

$$\mathbb{I}[g_{\perp}(\mathbf{x}) \geq \max_k g_k(\mathbf{x})]$$

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cross-entropy loss^(*)

$$\begin{aligned} \ell(\theta; \mathbf{x}, y, m) \\ = -\log h_y(\mathbf{x}) - \mathbb{I}[y = m] \log h_{\perp}(\mathbf{x}) \end{aligned}$$

incurred if expert correct

(*) other parameterizations/surrogate losses possible

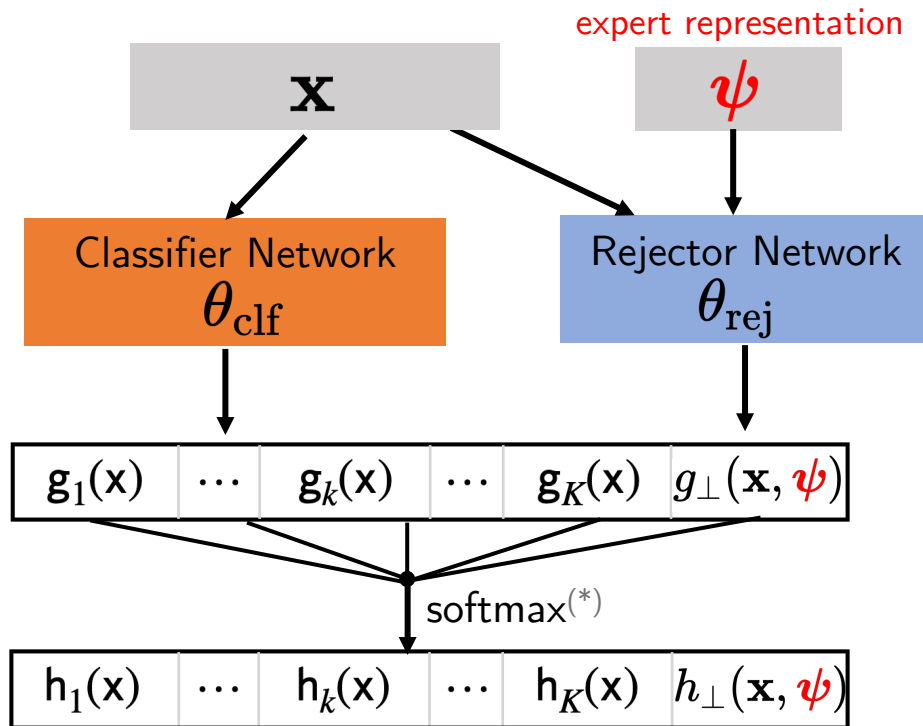
Learning to Defer to a Population

training data

$$\mathcal{D} = \left\{ \mathbf{x}_n, y_n, \{m_{n,e}, \psi_e\}_{e=1}^{E_n} \right\}_{n=1}^N$$

multiple expert demonstrations & representations

Learning to Defer to a Population



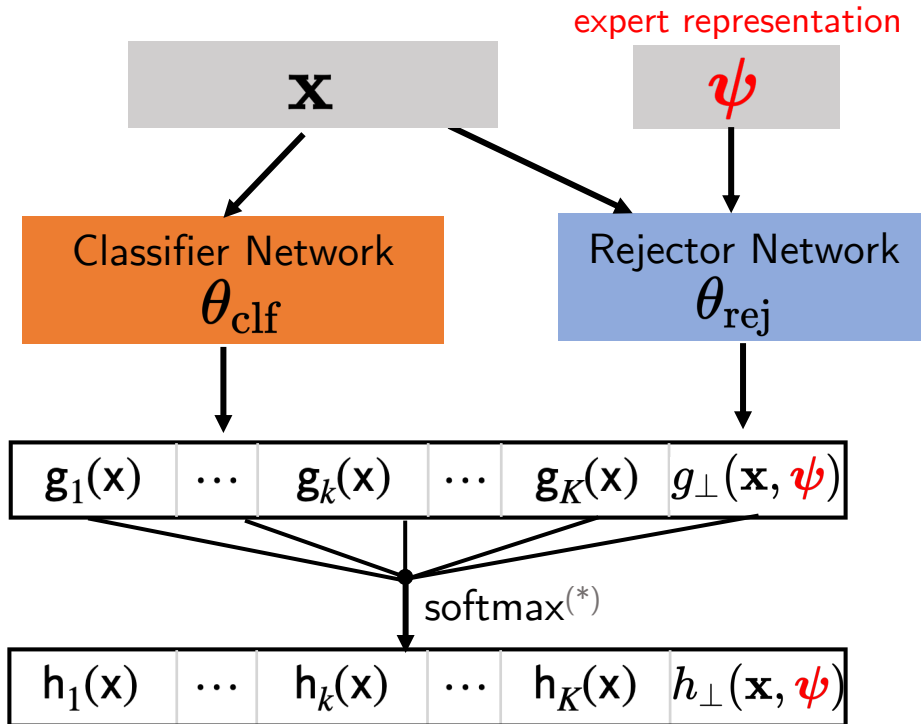
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Meta-Learning to Defer

representative set of
expert demonstrations /
“context set”

training data

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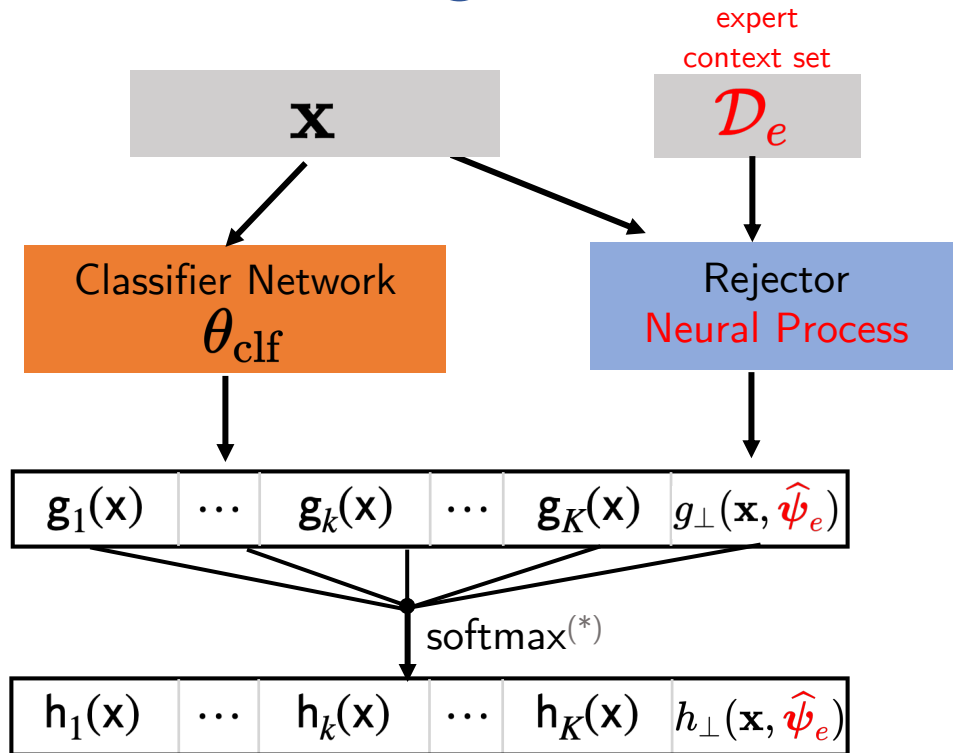
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Amortized expert representation as set embedding

$$\begin{aligned} \hat{\psi}_e &= \psi(\mathcal{D}_e) \\ &= \rho \left(\sum_{b=1}^B f_{\theta}(\mathbf{x}_{e,b}, y_{e,b}, m_{e,b}) \right) \end{aligned}$$

Meta-Learning to Defer



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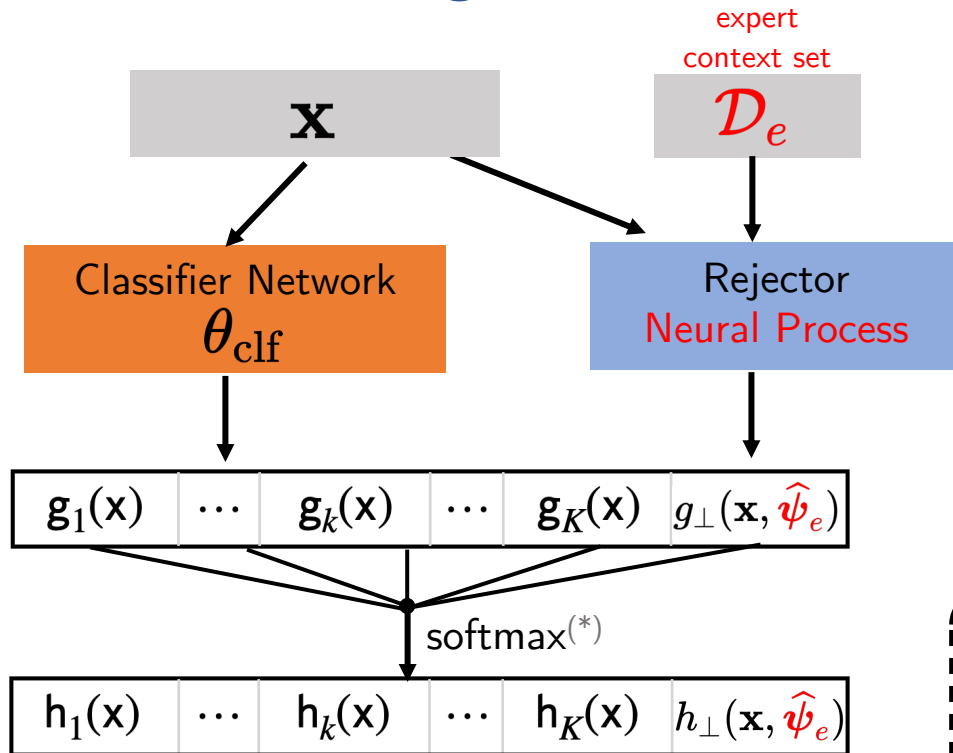
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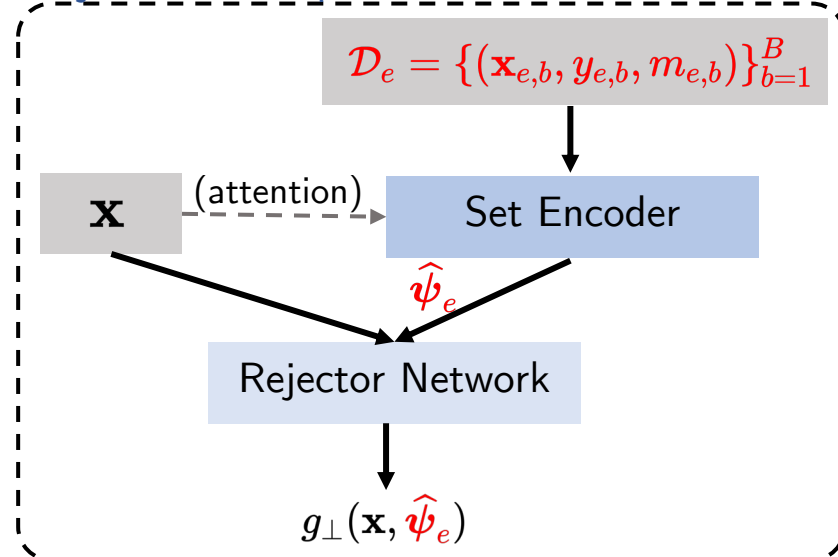
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rejector neural process



Zaheer et. al. *Deep Sets*. NeurIPS, 2017.

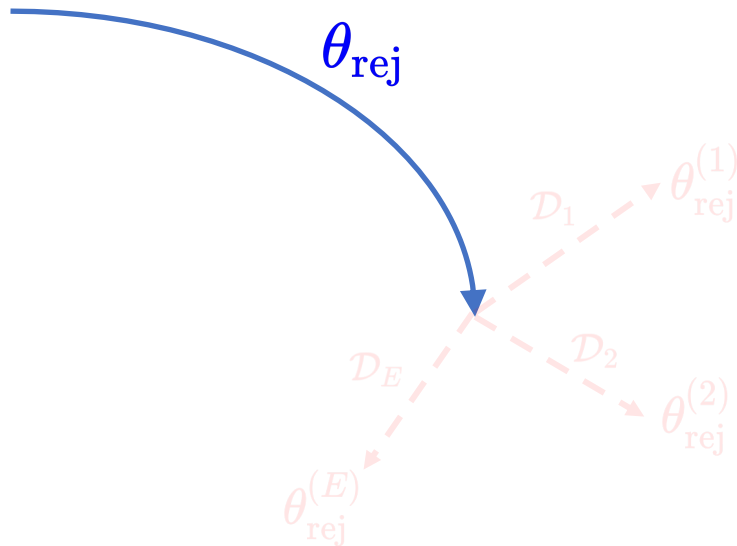
Garnelo et. al. *Conditional Neural Processes*. ICML, 2018.

Fine-tuning from marginal expert

training data

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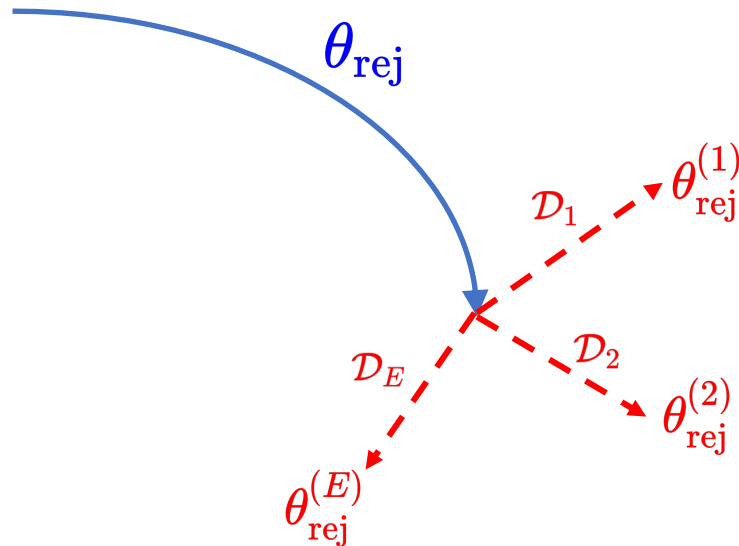
1. Model the *marginal* expert by the single-expert formulation

Fine-tuning from marginal expert

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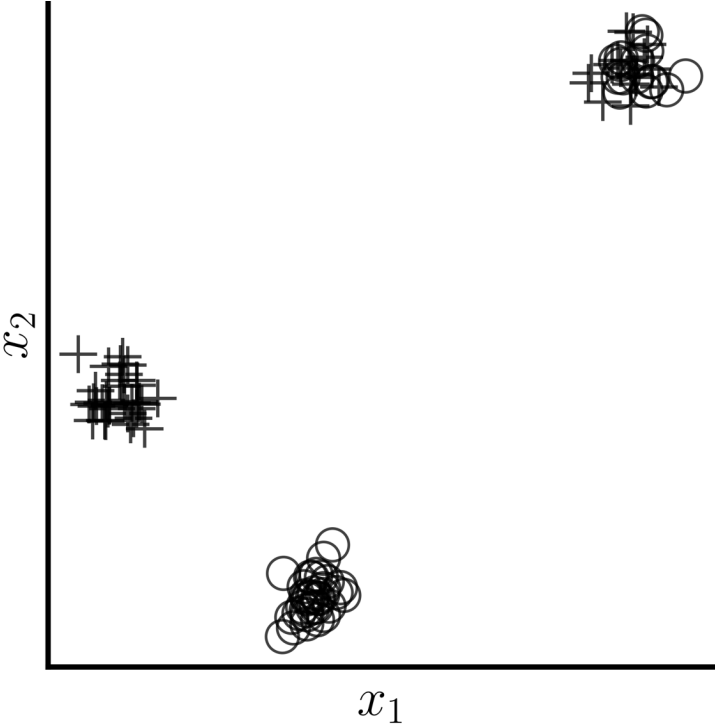
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1. Model the *marginal* expert by the single-expert formulation
2. Then finetune on expert context set at test-time

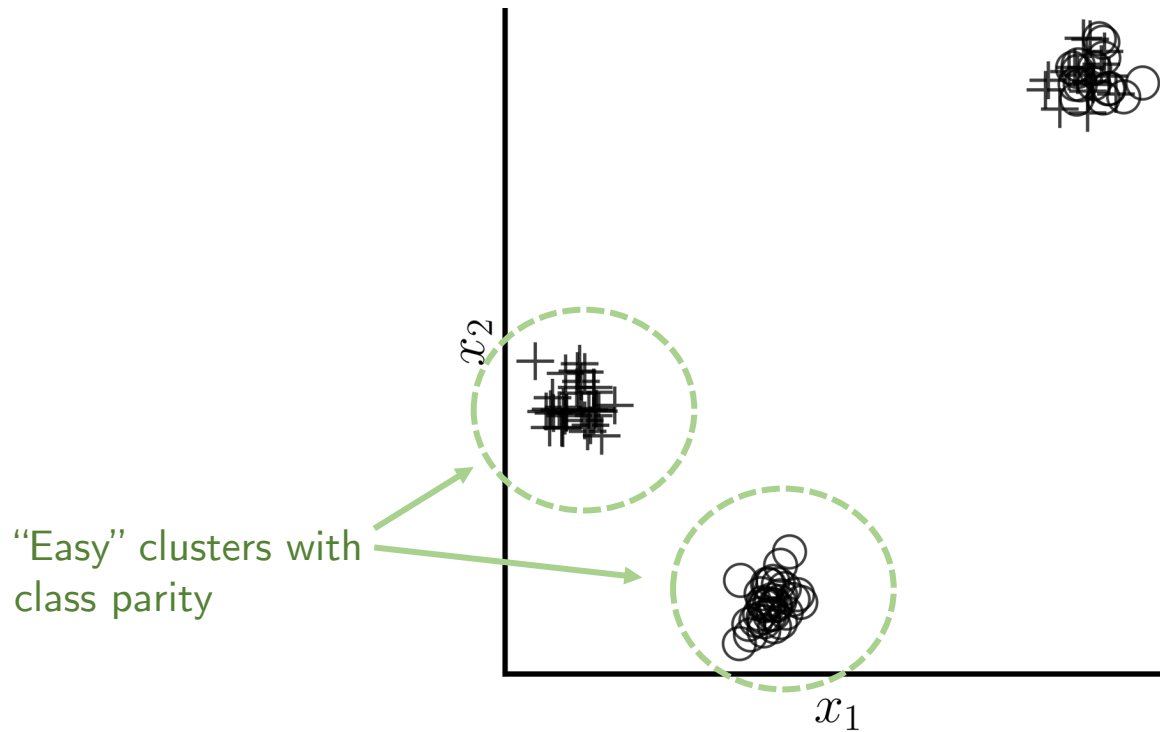
Experiment: Synthetic data

+ : class 0 O : class 1



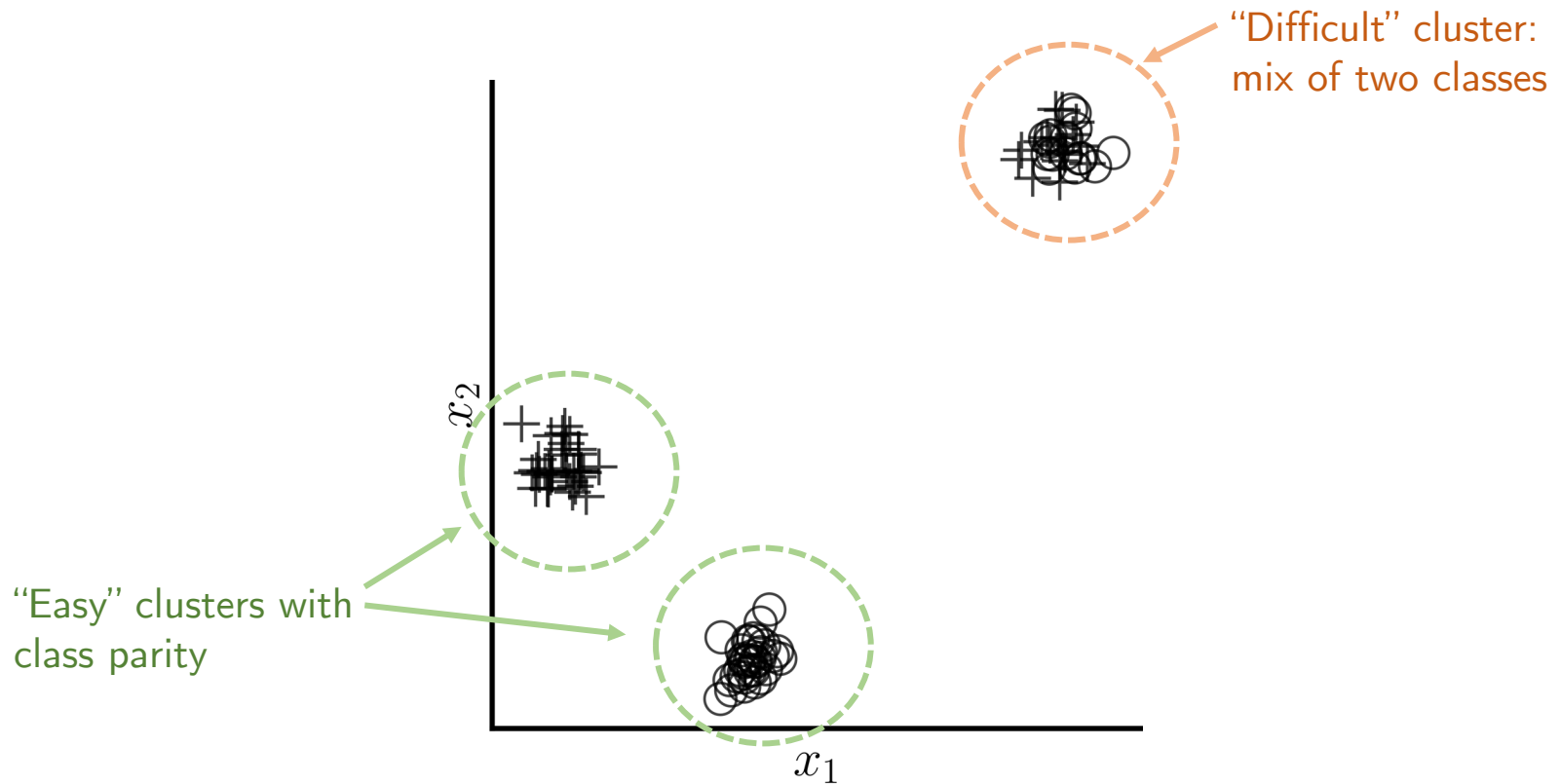
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Experiment: Synthetic data

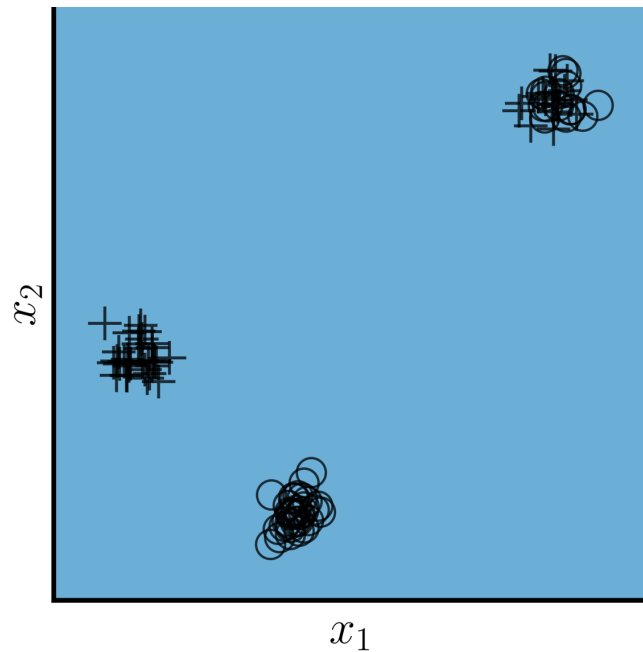
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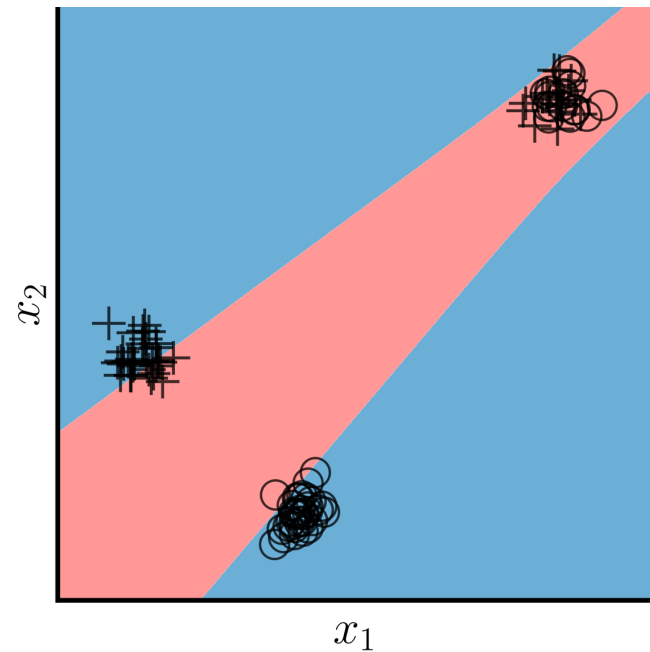
Experiment: Synthetic data

+ : class 0 O : class 1  L2D-Pop classifier region  L2D-Pop deferral region



Unskilled expert (1% accuracy)



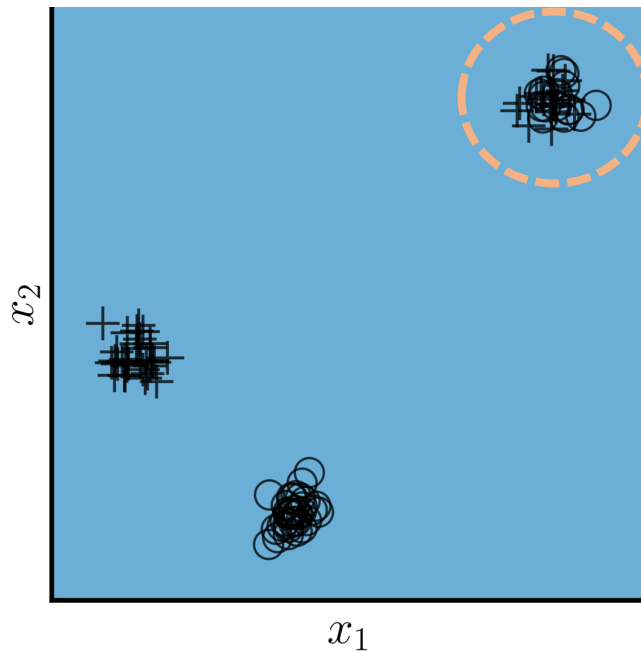
Skilled expert (95% accuracy)



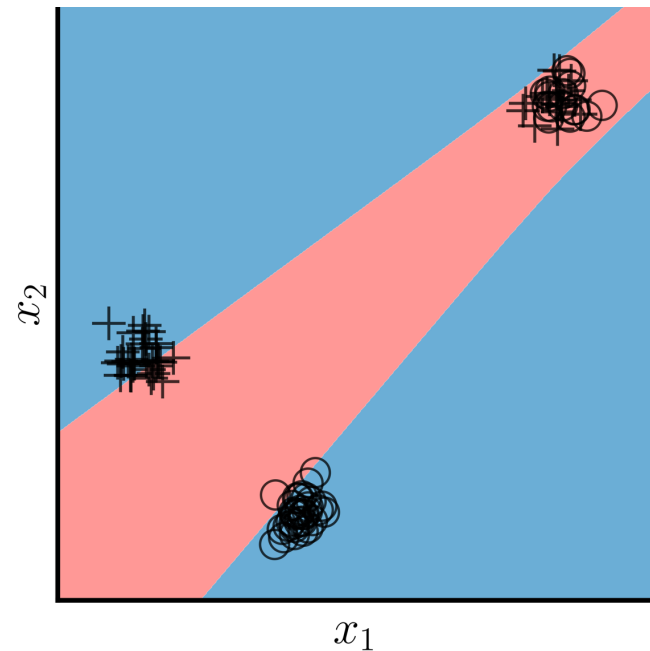
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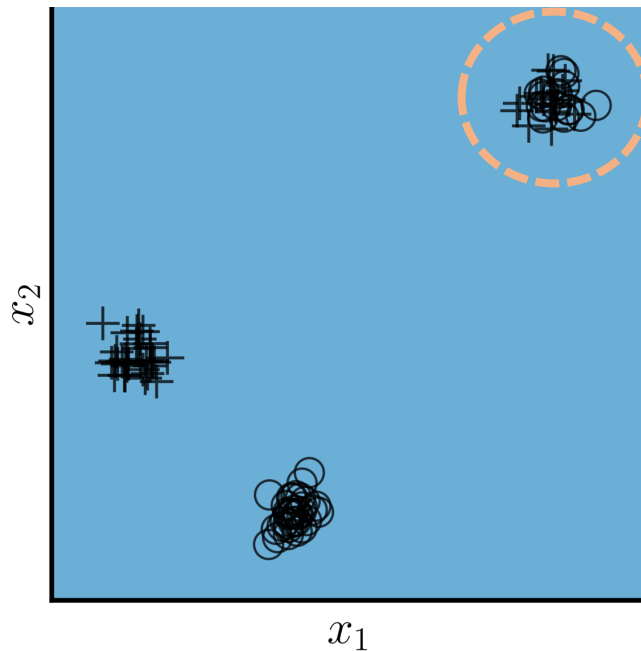


L2D-Pop (adaptive) ✓ Doesn't defer when the expert is poor

Experiment: Synthetic data

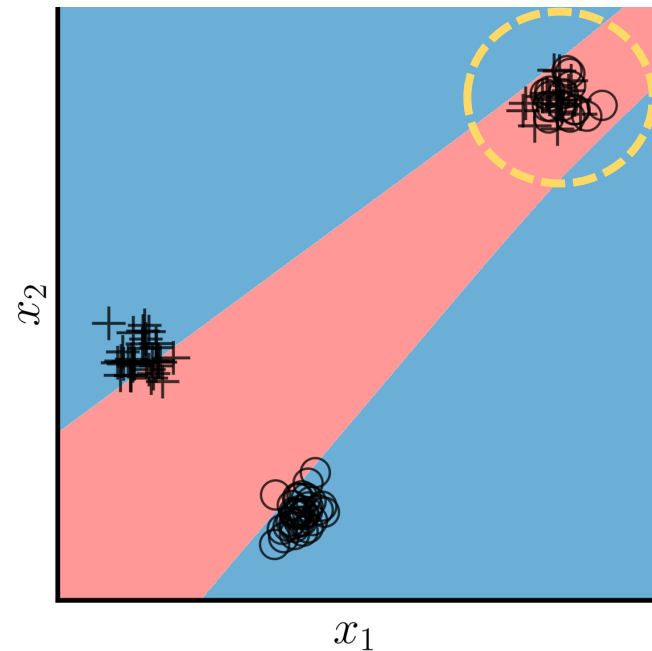
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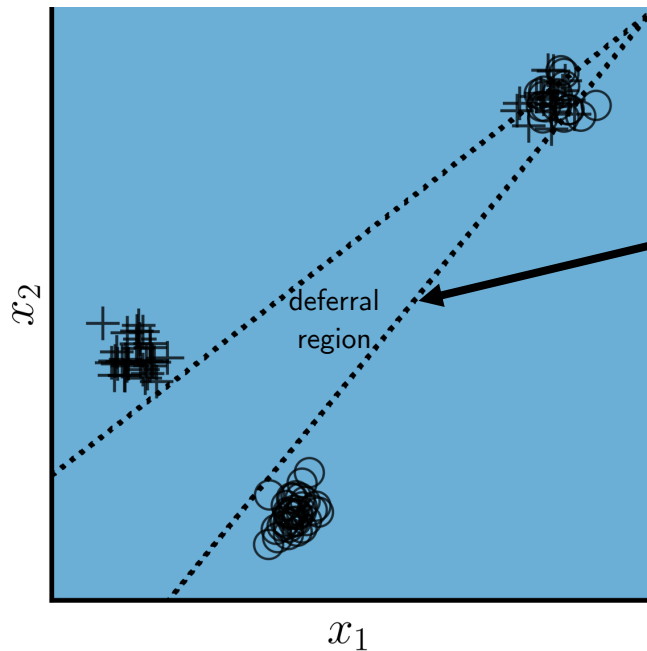


✓ Defers whole of difficult cluster when expert is good

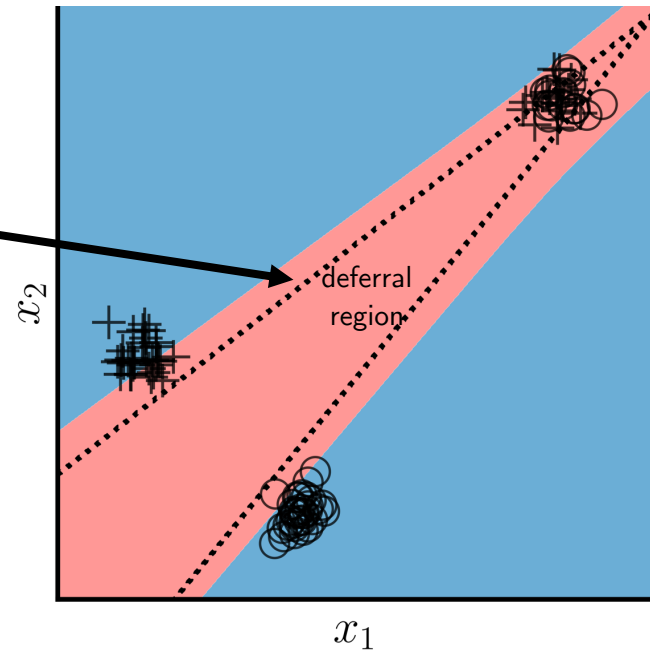
Experiment: Synthetic data

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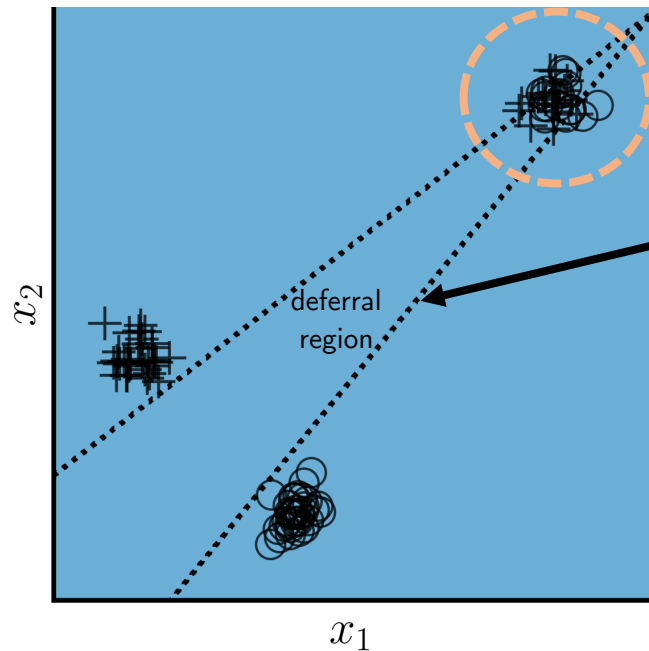
L2D-Pop (adaptive) ✓ Doesn't defer when the expert is poor

✓ Defers whole of difficult cluster when expert is good

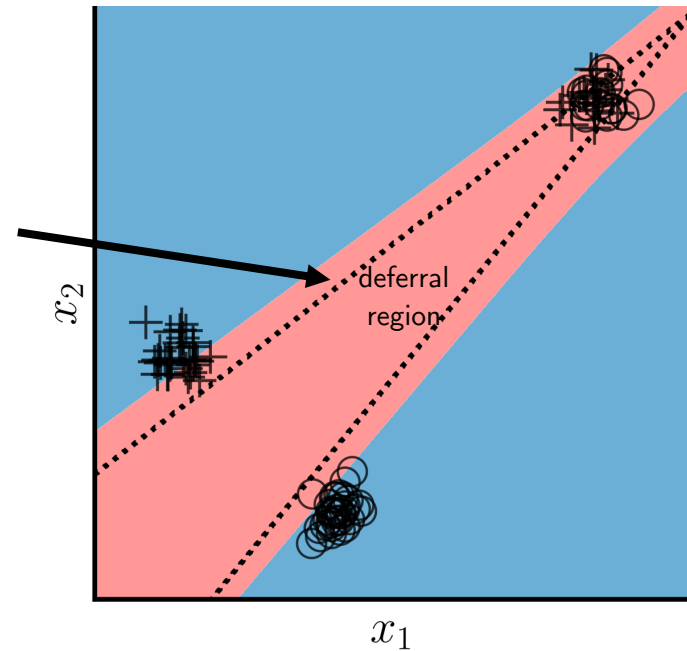
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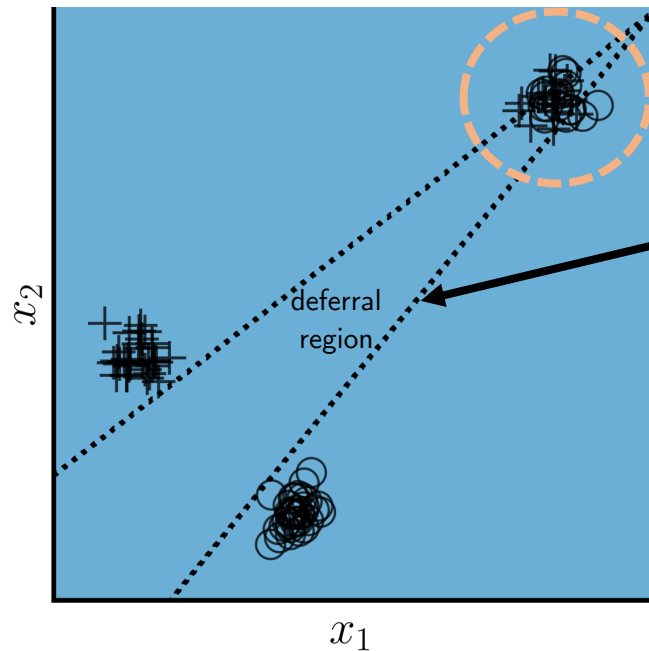
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single-L2D (constant) ✗ Over-defers as expert does worse than random on difficult cluster

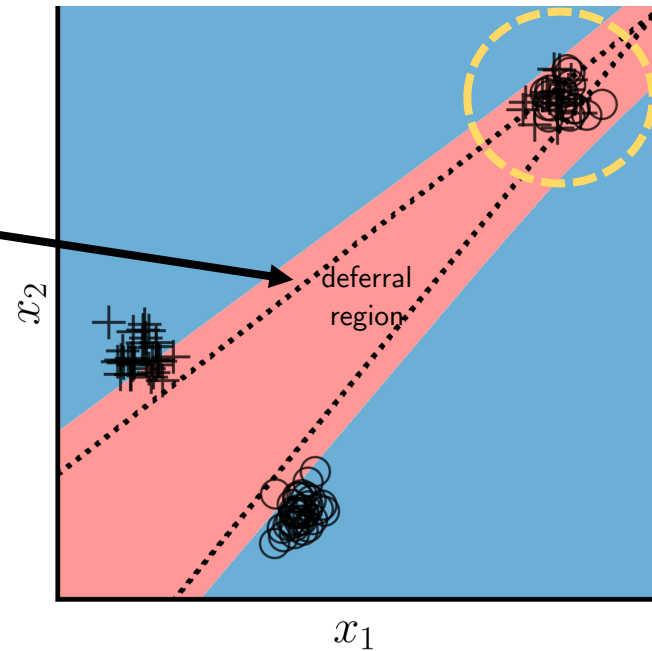
Experiment: Synthetic data

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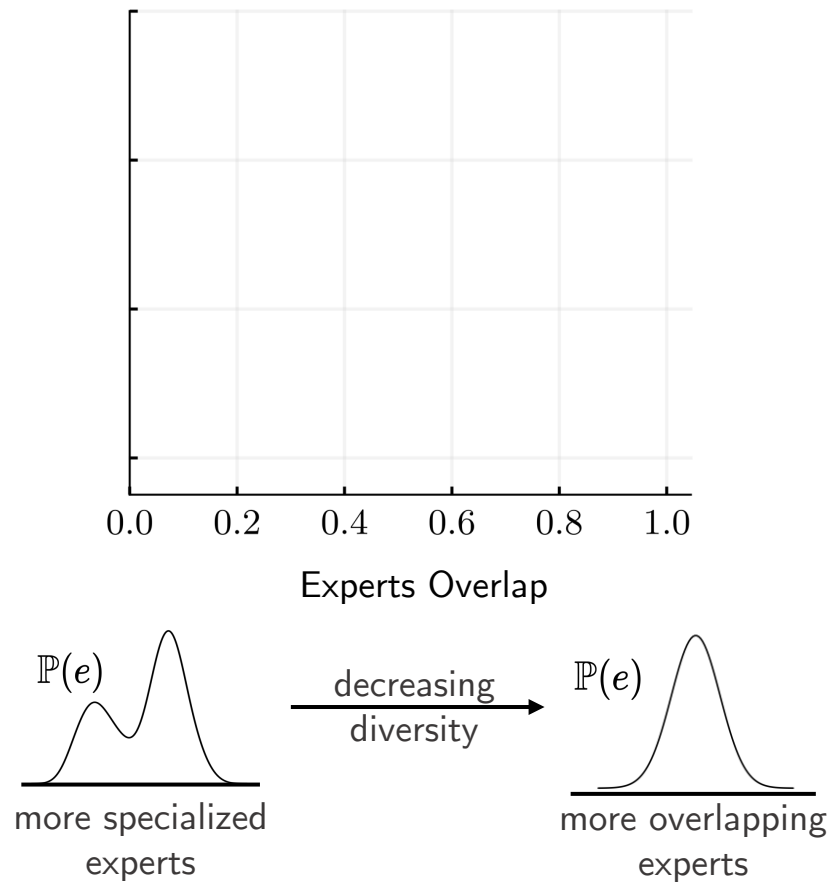
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✓ Defers whole of difficult cluster when expert is good

✗ Under-defers as classifier only has random chance of being correct on difficult cluster

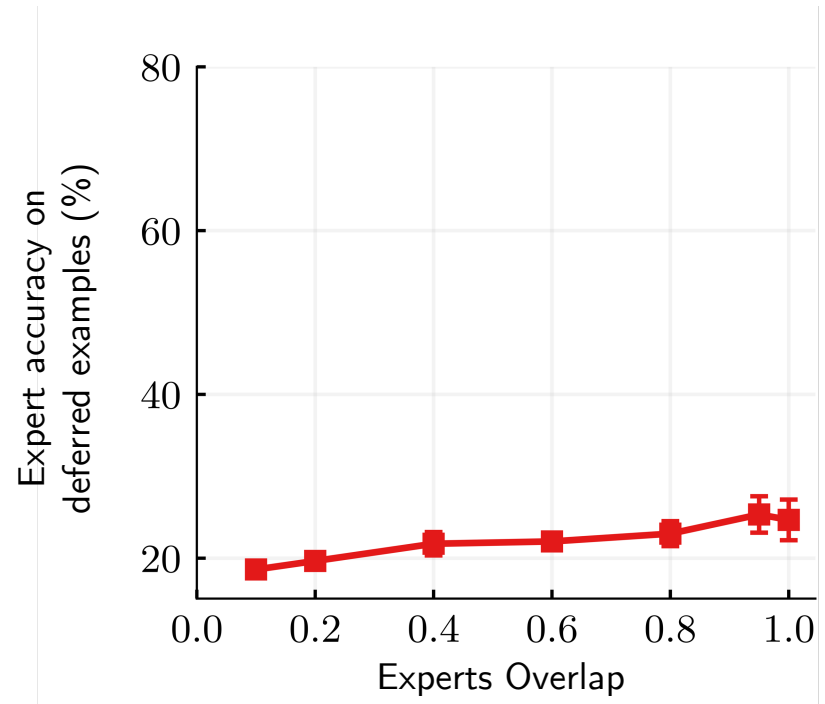
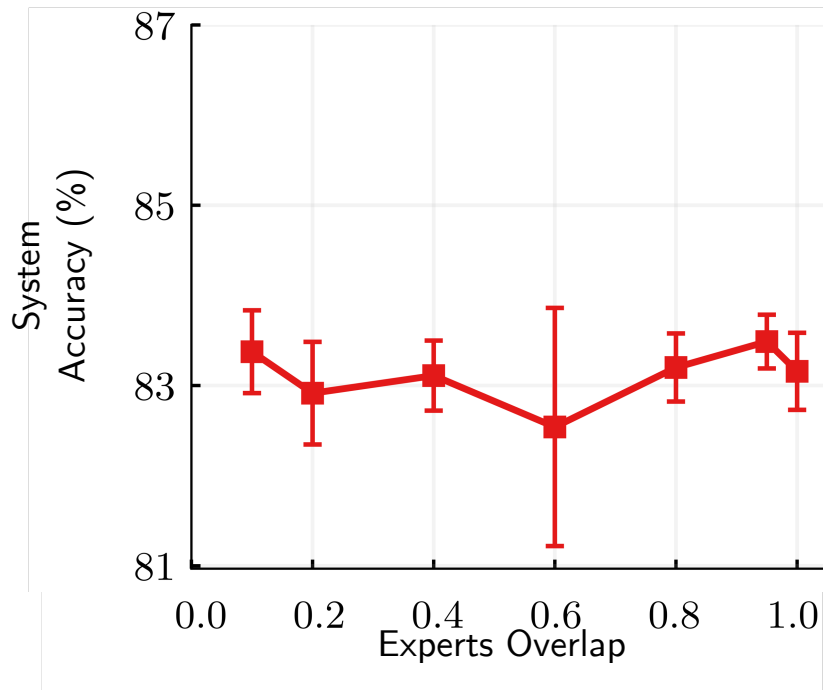
Experiments: Varying Population Diversity



Experiments: Varying Population Diversity

CIFAR-20 results

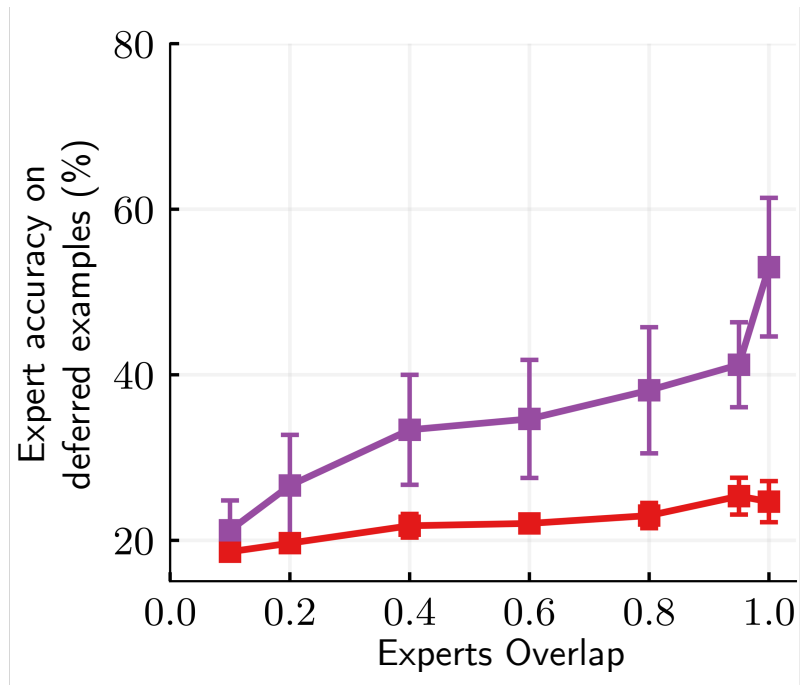
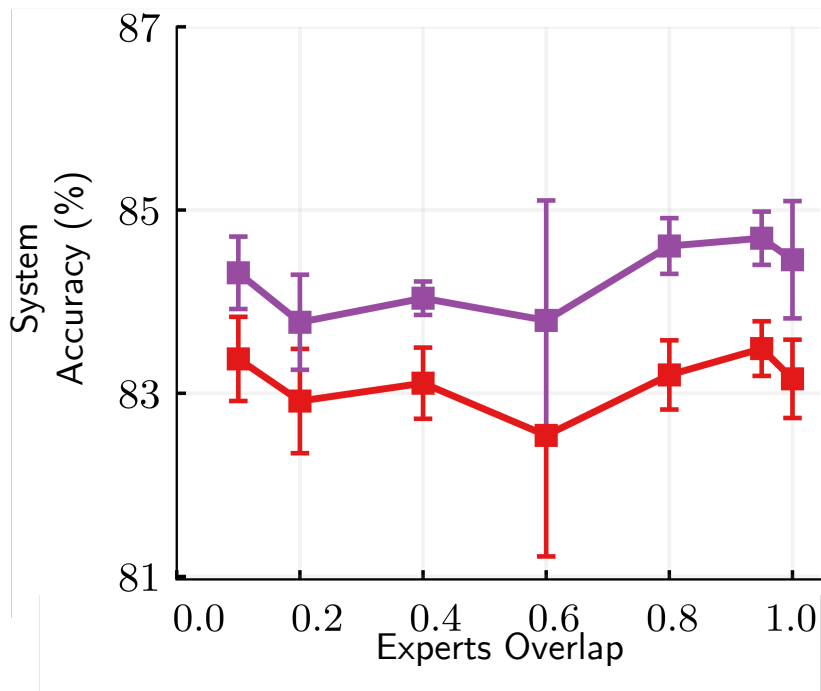
—■— single-L2D



Experiments: Varying Population Diversity

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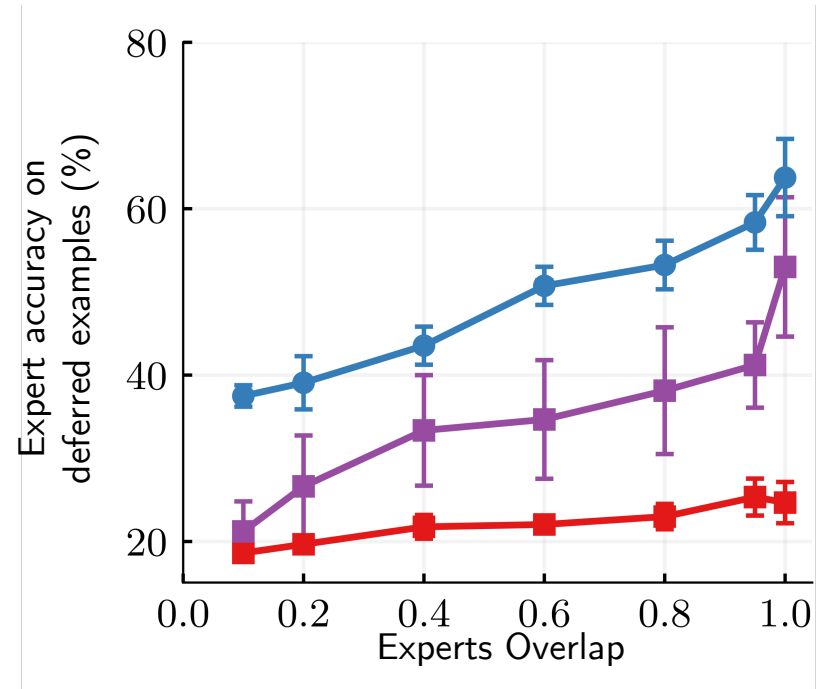
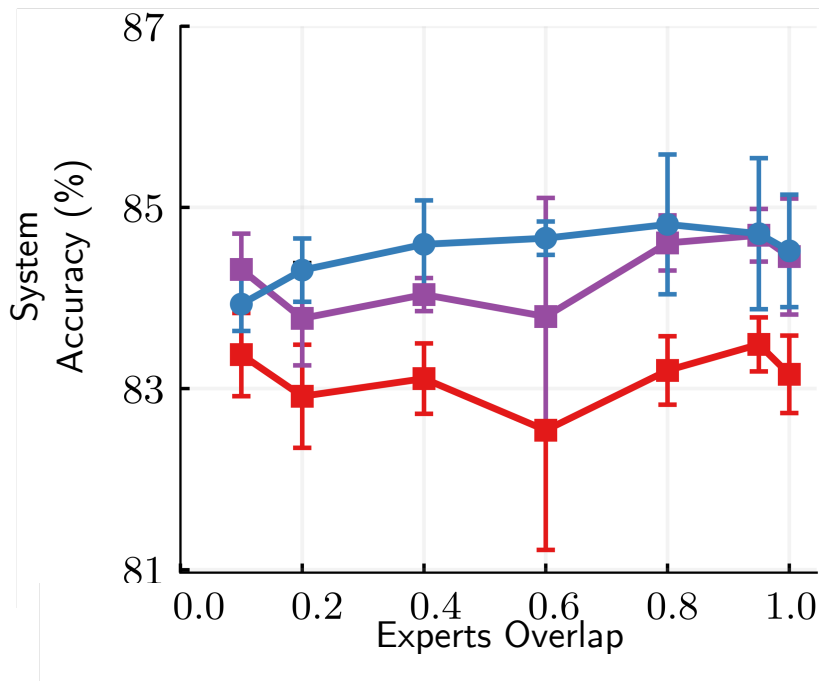
—■— single-L2D —■— L2D-Pop (finetune)



Experiments: Varying Population Diversity

CIFAR-20 results

—■— single-L2D —■— L2D-Pop (finetune) —●— L2D-Pop (NP)

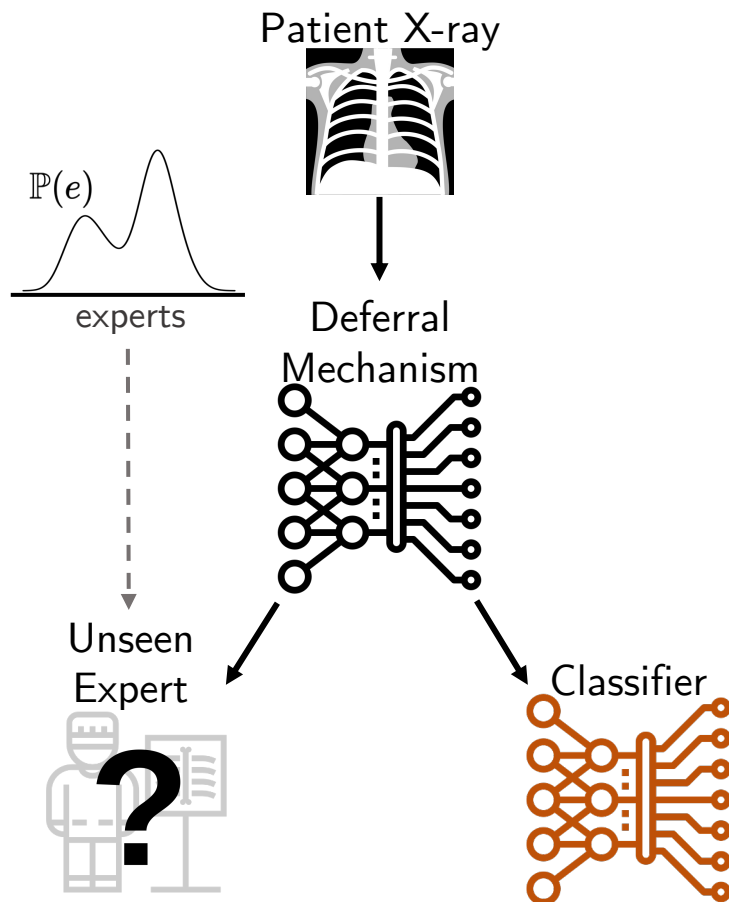


L2D-Pop is superior at deferring as shown by the expert accuracy on deferred examples (right) leading to a boost in system accuracy (left). The improvement is greater for the Neural Process implementation.

Further Experiments and Results

- **Further experiments in paper**
 - Additional benchmark problems: traffic sign detection and skin lesion diagnosis
 - Using OvA surrogate
- **Consistency of softmax and OvA surrogate loss functions for L2D-Pop**
- **Attentive neural process** implementation of L2D-Pop
- **Model-agnostic meta-learning (MAML)** implementation of L2D-Pop

Learning to Defer to a Population: A Meta-Learning Approach



Thank you!

